Q1. Given that MTBF=2000 hours and MTTR=4 Hours, calculate unavailability for single and dual processor systems in 30 years of exchange operation.

Ans:
$\mathrm{U}=4 / 2000$
$=2 * 10^{-3}$
In 30 years of operation total hours $=30 * 365.25 * 24 * \mathrm{U}$
$=525.96$ hours in 30 years
$U_{D}=2 * 16 / 2000 * 2000$
$=8 * 10^{-6}$
In 30 years of operation total hours $=30 * 365.25 * 24 * U_{D}$
$=2.10384$ hours in 30 years

## Q2. Differentiate between single stage and multistage networks

Ans:

| S.No. | Single stage | Multistage |
| :---: | :---: | :---: |
| 1. | Inlet to outlet connection is through a single crosspoint. | Inlet to outlet connection is through multiple crosspoints. |
|  | Use of a single crosspoint per connection results in better quality link. | Use of multiple crosspoints may degrade the quality of a connection. |
|  | Each individual crosspoint can be used for only one inlet/outlet pair connection. | Same crosspoint can be used to establish connection between a number of inlet/outlet pairs. |
| 4. | A specific crosspoint is needed for each specific connection. | A specific connection may be established by using different sets of crosspoints. |
|  | If a crosspoint fails, associated connection cannot be established. There is no redundancy. | Alternative cross-points and paths are available. |
|  | Crosspoints are inefficiently used. Only one crosspoint in each row or column of a square or triangular switch matrix is ever in use, even if all the lines are active. | Crosspoints are used efficiently. |
|  | Number of crosspoints is prohibitive. | Number of crosspoints is reduced significantly. |
|  | A large number of crosspoints in each inlet/outlet leads to to capacitive loading. | There is no capacitive loading problem. |
|  | The network is nonblocking in character. | The network is blocking in character. |
| 10. | Time for establishing a call is less. | Time for establishing a call is more. |

## Q3. Explain Three Stage Network with the help of diagram

Ans:

## Three-Stage Networks

The blocking probability and the number of switching elements can be reduced significantly by adopting a three-stage structure in place of two-stage networks. The general structure of an $N \times N$ three-stage blocking network is shown

The $N$ inlets and $N$ outlets are divided into $r$ blocks of $p$ inlets and $p$ outlets each respectively. The network is realised by using switching matrices of size $p \times s$ in stage $1, r \times r$ in stage 2 , and $s \times p$ in

$N \times N$ three-stage switching network.
stage 3. Unlike the two-stage network discussed
here any arbitrary inlet in the first stage has $s$ alternative paths to reach any arbitrary outlet in the third stage. The total number of switching elements is given by

$$
S=r p s+s r^{2}+s p r=2 N s+s r^{2}=s\left(2 N+r^{2}\right)
$$

If we use square matrices in the first and third stages, we have $p=s=(N / r)$ and, therefore,

$$
S=\frac{2 N^{2}}{r}+N r
$$

Equation (4.15) indicates that there is an optimum value for $r$ that would minimise the value of $S$. To obtain this value of $r$, we differentiate set it equal to zero and determine the value of $r$ :

$$
\frac{d S}{d r}=\frac{-2 N^{2}}{r^{2}}+N=0
$$

Therefore, $r=\sqrt{2 N}$. The second derivative, being positive at this value of $r$, indicates that the value of $S$ is minimum, i.e.

$$
S_{\min }=2 N \sqrt{2 N}
$$

and $p=N / r=\sqrt{N / 2}$. The optimum ratio of the number of blocks to the number of inputs per block is given by

$$
r / p=\sqrt{2 N} / \sqrt{N / 2}=2
$$

