

- Q1. Explain the concept of information in "Information Theory"?
- Q2. Explain the concept of "Entropy"?
- Q3. What is multiplexing? Explain Time division multiplexing?

### Solutions

Ans: Q1] Information :-

Let us consider a communication system in which the allowable messages are  $m_1, m_2, \dots, m_n$ , with probabilities of occurrence  $P_1, P_2, \dots, P_m$

$$P_1 + P_2 + \dots + P_m = 1 \quad \text{--- (1)}$$

If probability of occurrence of a symbol is  $P[x_i]$  then information associated with that symbol is;

$$I[x_i] \propto \frac{1}{P[x_i]} \quad \text{--- (2)}$$

$$I[x_i] = \log_b \left[ \frac{1}{P[x_i]} \right]$$

$$I[x_i] = -\log_b(P[x_i]) \quad \text{--- (3)}$$

unit of the information depends upon the base ( $b$ ) of log.

Base ( $b$ )	unit
2	bit
e	nat
10	decit

If the probability of occurrence of a symbol is high, then information associated with it will be less and vice versa.

## # Properties of $I(x_i)$ :-

(Q) The information contained by a symbol  $x_i$ , denoted by  $I(x_i)$  satisfies the following properties -

①.  $I(x_i^0) = 0$  ; if  $P(x_i^0) = 1$

• A certain event conveys zero information.

②.  $I(x_i^0) \geq 0$  ; Information can not be negative.

③.  $I(x_i^0) > I(x_j^0)$  if  $P(x_i^0) < P(x_j^0)$

Events having more certainty contains less information.

(Q2) What is the concept of "Entropy"?

ANS:- Entropy:-

Entropy tells that how many bits of information is contained by each symbol.

Unit of Entropy is  $\Rightarrow$  (Bits/symbol)

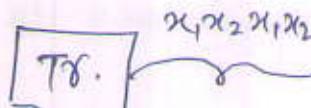
$$\text{Entropy } H = \sum_i I(x_i^0) \cdot P[x_i^0] \text{ bits/symbol.} \rightarrow ①$$

$$\text{we know that } I(x_i^0) = \log_2 \left[ \frac{1}{P(x_i^0)} \right] \text{ bits.} \rightarrow ②$$

$$\Rightarrow H = \sum_i P[x_i^0] \cdot \log_2 \left( \frac{1}{P(x_i^0)} \right)$$

$$\Rightarrow \boxed{H = - \sum_i P(x_i^0) \cdot \log_2 [P(x_i^0)]} \text{ Bits/symbol.}$$

Case(A)

 Tx. is transmitting two symbols.

Q1. Let  $P(x_1) = P(x_2) = \frac{1}{2}$

$$\Rightarrow H = \sum_{i=1}^2 P(x_i^0) \cdot \log_2 \left( \frac{1}{P(x_i^0)} \right)$$

$$H = \frac{1}{2} \log_2(2) + \frac{1}{2} \log_2(2)$$

$$\Rightarrow \boxed{H = 1} \text{ bits/symbol}$$

(ii)  $P(x_1)=1; P(x_2)=0$  it means fr. is only transmitting symbol  $x_1$ , and not  $x_2$

$$H = \sum_{i=1}^2 P(x_i) \cdot \log_2 \left( \frac{1}{P(x_i)} \right)$$

$$H = - \sum_{i=1}^2 P(x_i) \cdot \log_2 [P(x_i)]$$

$$H = -1 \cdot \log_2 (1) + 0 \cdot \log_2 (0)$$

$$\Rightarrow H = 0 \text{ bits/symbol}$$

case (B): Transmitter is transmitting three symbols:-

① Let  $P(x_1) = P(x_2) = P(x_3) = \frac{1}{3}$

$$H = \sum_{i=1}^3 P(x_i) \cdot \log_2 \left( \frac{1}{P(x_i)} \right)$$

$$H = \frac{1}{3} \cdot \log_2 (3) + \frac{1}{3} \cdot \log_2 (3) + \frac{1}{3} \log_2 (3)$$

$$\Rightarrow H = \log_2 3 \text{ bits/symbol}$$

②.  $P(x_1)=1; P(x_2)=P(x_3)=0$

$$\Rightarrow H = 0 \text{ bits/symbol.}$$

③.  $P(x_1)=\frac{1}{2}; P(x_2)=\frac{1}{2}; P(x_3)=0$

$$\Rightarrow H = \frac{1}{2} \cdot \log_2 (2) + \frac{1}{2} \log_2 (2) + 0$$

$$\Rightarrow H = 1 \text{ Bits/symbol}$$

Generalised case:-

Let Transmitter is transmitting  $m$  such symbols such that

$$P(x_1) = P(x_2) = \dots = P(x_m) = \frac{1}{m}$$

$$H = \frac{1}{m} \cdot \log_2 m + \frac{1}{m} \cdot \log_2 m + \dots \quad m \text{ times}$$

$$\Rightarrow H = \log_2 m \text{ Bits/symbol.}$$

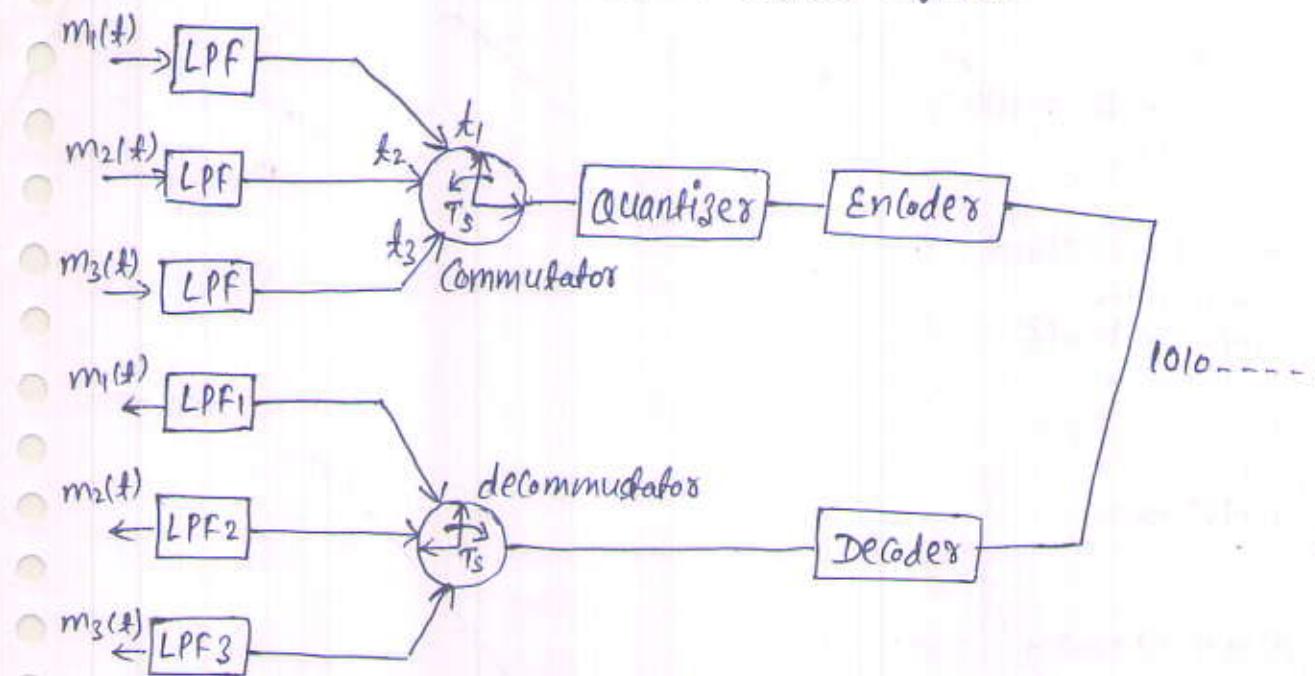
Q3). What is multiplexing? Explain Time division multiplexing (TDM)?

Sol). Multiplexing:-

Multiplexing is the process of transmitting multiple number of signals through a single channel at the same time.

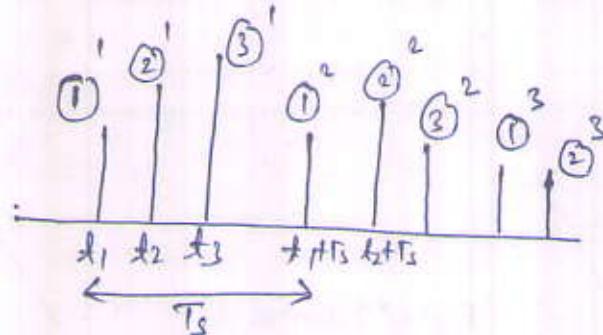
## # Time division multiplexing (TDM) :-

TDM is used to multiplex digital signals.



- ① Low Pass filters are used as Anti-Aliasing filter.
- ② Commutator is a Rotating switch which rotates in Anti-clockwise direction with uniform speed.
- ③ Time taken by Commutator to make one complete rotation is identified as "frame time" ( $T_s$ ).
- ④ Commutator is used to sample multiple no. of continuous signals.

Commutator o/p.



Let No. of signals multiplexed =  $N$

No. of bits required to represent each sample =  $n$

$$T_s = N \cdot n \cdot T_b$$

$T_b \rightarrow$  Pulse width.

$$\Rightarrow T_b = \frac{T_s}{N \cdot n} \text{ sec.}$$

$$\text{Bit Rate } R_b = \frac{1}{T_b}$$

$$\Rightarrow R_b = N \cdot n \cdot f_s$$