

**J.D.B Govt. Girls College, Kota**  
**Sample Question Paper**  
**B.Sc. Part III**  
**P-I Linear algebra and Complex analysis**

Max. Marks-20

Q.1 Attempt all questions(each question for 01 marks)

- (a) Define the Harmonic function?
- (b) If in a domain harmonic functions  $u$  and  $v$  satisfy C-R equations, then  $u+iv$  is an analytic function in that domain?
- (c) Write the procedure to determine the conjugate function?
- (d) Find the harmonic conjugate of  $u(x, y)=2x(1-y)$ ?
- (e) Prove that the function  $u(x, y)=e^x (x \cos y - y \sin y)$ .

Q.2 Short answer questions (each question for 02 marks)

- (a) Define Milne Thomson Method?
- (b) If  $(u-v) = (x-y)(x^2+4xy+y^2)$  and  $f(z)= u+iv$  is an analytic function of  $z=x+iy$ , find  $f(z)$  in terms of  $z$ .
- (c) Show that an analytic function with constant modulus is constant.
- (d) If  $f(z)$  is analytic, then prove that
- (e) If  $f(z)$  is analytic, then prove that  $\left(\frac{\partial^2}{\partial x^2} + \frac{\partial^2}{\partial y^2}\right) |f(z)|^2 = 4|f'(z)|^2$

Q.3 Descriptive Questions (05 marks)

- (a) Derive the methods to construct an analytic function when one conjugate function is given?

**Janki Devi Bajaj Government Girls College, Kota**  
**Sample Question Paper**  
**B.Sc. Part III**  
**P-II Mathematical statistics and linear programming**

Max. Marks-20

Q.1 Attempt all questions

- (a) Prove that dual of a dual is a prime number
- (b) Define assignment problem.
- (c) Define fundamental theorem of duality in L.P.P
- (d) Define infeasible assignment
- (e) Write the dual of the following problem

$$\begin{aligned} \text{Min } z &= 3x_1 + x_2 \\ x_1 + x_2 &\geq 1 \\ 2x_1 + 3x_2 &\geq 2 \\ x_1, x_2 &\geq 0 \end{aligned}$$

Q.2 Short answer questions

- (a) Describe mathematical formulation of assigned problem.
- (b) solve the following assignment problem

	Jobs	→				
Persons			<b>I</b>	<b>II</b>	<b>III</b>	<b>IV</b>
↓	<b>A</b>	2	3	4	5	
	<b>B</b>	4	5	6	7	
	<b>C</b>	7	8	9	8	
	<b>D</b>	3	5	8	4	

(c) Find the DP of the following LPP,

$$\begin{aligned} \text{Max } z &= 2x_1 + 3x_2 + x_3 \\ \text{s.t} \quad &4x_1 + 3x_2 + x_3 = 6 \\ &x_1 + 2x_2 + 5x_3 = 4 \\ &\& \quad x_1, x_2, x_3 \geq 0 \end{aligned}$$

(d) Find the DP of the following LPP,

$$\begin{aligned} \text{Min } z &= x_1 + x_2 + x_3 \\ \text{s.t} \quad &x_1 - 3x_2 + 4x_3 = 5 \end{aligned}$$

$$\begin{aligned}2x_1 - 2x_2 &\leq -3 \\ 2x_2 - x_3 &\geq 5\end{aligned}$$

&  $x_1, x_2 \geq 0$  ,  $x_3$  is unrestricted in sign.

(e) State & prove the reduction theorem of assignment.

### Q.3 Descriptive Questions

(a) Use DP to solve the following LPP,

$$\begin{aligned}Min z &= 3x_1 + x_2 \\ x_1 + x_2 &\geq 1 \\ 2x_1 + 3x_2 &\geq 2 \\ x_1, x_2 &\geq 0\end{aligned}$$

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**Sample Question Paper**  
**B.Sc. Part III**  
**P-III Numerical Analysis & C-Programming**

Max. Marks-20

Q.1 Attempt all questions

- (a) Define Boundary condition
- (b) Define initial value problem.
- (c) Write formula of Picard's method.
- (d) Define Ordinary differential equation.
- (e) Write formula of Euler's method.

Q.2 Short answer questions

- (a) Use Picard's method to solve  $\frac{dy}{dx} = 1 + xy$  passing through (0,1), correct to three places of decimal for  $x=0.1$
- (b) Use Picard's method to solve  $\frac{dy}{dx} = 1 + xy$  passing through (0,1), with  $x_0=2, y_0=0$ .
- (c) Use Picard's method to solve  $\frac{dy}{dx} = x + y$  with  $x_0=x=0, y_0=y=1$
- (d) Given  $\frac{dy}{dx} = \frac{y-x}{y+x}$  with  $y=1$  for  $x=0$ , find  $y$  approximately for  $x=0.1$  by Euler's method(two steps)
- (e) Use Euler's method to solve  $\frac{dy}{dx} = \frac{y^2-x}{y^2+x}$ ,  $x=0, y=1$ , compute  $y(0.1)$ ,  $y(0.2)$ ,  $y(0.3)$

Q.3 Descriptive Questions

- (a) Use Euler's method with  $h=0.1$  to find the solution of the question

$$\frac{dy}{dx} = x^2 + y^2, \text{ with } y(0)=0, \text{ in the range } 0 \leq x \leq 0.5$$

