

Groot Women Polytechnic College, Bharatpur.

Q. 1. यदि $A = \begin{bmatrix} 0 & 1 \\ 1 & 0 \end{bmatrix}$ है तो सिद्ध करो $A^2 = I$

Ans $\Rightarrow A = \begin{bmatrix} 0 & 1 \\ 1 & 0 \end{bmatrix}$

To Prove $A^2 = I$

$$A^2 = A \times A = \begin{bmatrix} 0 & 1 \\ 1 & 0 \end{bmatrix} \times \begin{bmatrix} 0 & 1 \\ 1 & 0 \end{bmatrix}$$

$$A^2 = \begin{bmatrix} 0+1 & 0+0 \\ 0+0 & 1+0 \end{bmatrix}$$

$$A^2 = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} = I \quad \text{Proved that.}$$

Q2 यदि $A = \begin{bmatrix} 0 & 2 & 3 \\ 2 & 1 & 4 \end{bmatrix}$ व $B = \begin{bmatrix} 7 & 6 & 3 \\ 1 & 4 & 5 \end{bmatrix}$ है तो $3A-B$ का मान निकालो।

Ans $\Rightarrow A = \begin{bmatrix} 0 & 2 & 3 \\ 2 & 1 & 4 \end{bmatrix}$

$$B = \begin{bmatrix} 7 & 6 & 3 \\ 1 & 4 & 5 \end{bmatrix}$$

$$3A - B = ?$$

$$\Rightarrow 3A - B = 3 \begin{bmatrix} 0 & 2 & 3 \\ 2 & 1 & 4 \end{bmatrix} - \begin{bmatrix} 7 & 6 & 3 \\ 1 & 4 & 5 \end{bmatrix}$$

$$3A - B = \begin{bmatrix} 0 & 6 & 9 \\ 6 & 3 & 12 \end{bmatrix} - \begin{bmatrix} 7 & 6 & 3 \\ 1 & 4 & 5 \end{bmatrix}$$

$$3A - B = \begin{bmatrix} -7 & 0 & 6 \\ -5 & -1 & 7 \end{bmatrix} \text{ Ans}$$

Q-3 x, y, z व t का मान ज्ञात करो यदि

$$\begin{bmatrix} x+3 & 2y+x \\ z-1 & 4t-6 \end{bmatrix} = \begin{bmatrix} 0 & -7 \\ 3 & 2t \end{bmatrix}$$

Ans \Rightarrow
$$\begin{bmatrix} x+3 & 2y+x \\ z-1 & 4t-6 \end{bmatrix} = \begin{bmatrix} 0 & -7 \\ 3 & 2t \end{bmatrix}$$

$$x+3 = 0 \quad \text{--- (1)}$$

$$2y+x = -7 \quad \text{--- (2)}$$

$$z-1 = 3 \quad \text{--- (3)}$$

$$4t-6 = 2t \quad \text{--- (4)}$$

= (4) से -

$$4t - 6 = 2t$$

$$4t - 2t = 6$$

$$2t = 6$$

$$t = \frac{6}{2}$$

$$\boxed{t = 3}$$

(3) से -

$$z - 1 = 3$$

$$z = 3 + 1$$

$$\boxed{z = 4}$$

1) से

$$x + 3 = 0$$

$$\boxed{x = -3}$$

x का मान दो में रखने पर

$$2y + x = -7$$

$$2y - 3 = -7$$

$$2y = -7 + 3$$

$$2y = -4$$

$$y = -2$$

तब

$$\boxed{x = -3}$$

$$\boxed{y = -2}$$

$$\boxed{z = 4}$$

$$\boxed{t = 3}$$

Q-4 \Rightarrow यदि $A = \begin{bmatrix} 1 & 2 & 2 \\ 2 & 1 & 2 \\ 2 & 2 & 1 \end{bmatrix}$ हो तो सिद्ध करो की $A^2 - 4A + 5I_3 = 0$

Ans \Rightarrow $A = \begin{bmatrix} 1 & 2 & 2 \\ 2 & 1 & 2 \\ 2 & 2 & 1 \end{bmatrix}$

To Prove $\rightarrow A^2 - 4A + 5I_3 = 0$ — (1)

$$A^2 = A \times A = \begin{bmatrix} 1 & 2 & 2 \\ 2 & 1 & 2 \\ 2 & 2 & 1 \end{bmatrix} \times \begin{bmatrix} 1 & 2 & 2 \\ 2 & 1 & 2 \\ 2 & 2 & 1 \end{bmatrix}$$

$$A^2 = \begin{bmatrix} 1+4+4 & 2+2+4 & 2+4+2 \\ 2+2+4 & 4+1+4 & 4+2+2 \\ 2+4+2 & 4+2+2 & 4+4+1 \end{bmatrix}$$

$$A^2 = \begin{bmatrix} 9 & 8 & 8 \\ 8 & 9 & 8 \\ 8 & 8 & 9 \end{bmatrix}$$

$$\textcircled{v} \text{ सिद्ध करें, } A^2 - 4A + 5I_3 = 0$$

$$= \begin{bmatrix} 9 & 8 & 8 \\ 8 & 9 & 8 \\ 8 & 8 & 9 \end{bmatrix} - 4 \begin{bmatrix} 1 & 2 & 2 \\ 2 & 1 & 2 \\ 2 & 2 & 1 \end{bmatrix} + 5 \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} = 0$$

$$\begin{bmatrix} 9 & 8 & 8 \\ 8 & 9 & 8 \\ 8 & 8 & 9 \end{bmatrix} - \begin{bmatrix} 4 & 8 & 8 \\ 8 & 4 & 8 \\ 8 & 8 & 4 \end{bmatrix} + \begin{bmatrix} 5 & 0 & 0 \\ 0 & 5 & 0 \\ 0 & 0 & 5 \end{bmatrix} = 0$$

$$\begin{bmatrix} 9-4-5 & 8-8-0 & 8-8-0 \\ 8-8-0 & 9-4-5 & 8-8-0 \\ 8-8-0 & 8-8-0 & 9-4-5 \end{bmatrix} = 0$$

$$\begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{bmatrix} = 0 \quad \underline{\text{L.H.S} = \text{R.H.S}} \quad \text{Hence proved}$$

Q-5 सिद्ध करें कि $D = \begin{bmatrix} 1 & x & yz \\ 1 & y & zx \\ 1 & z & xy \end{bmatrix} = (x-y)(y-z)(z-x)$

Ans. $D = \begin{vmatrix} 1 & x & yz \\ 1 & y & zx \\ 1 & z & xy \end{vmatrix} = \begin{vmatrix} 1 & 1 & yz \\ 1 & 1 & zx \\ 1 & 1 & xy \end{vmatrix} \begin{vmatrix} x^2 & y^2 & z^2 \end{vmatrix}$

L.H.S लेते हैं -

$$= \begin{vmatrix} 1 & x & yz \\ 1 & y & zx \\ 1 & z & xy \end{vmatrix} = (x-y)(y-z)(z-x) = \text{R.H.S}$$

Hence proved.